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Citation: *Physics of Plasmas* **24**, 073108 (2017); doi: 10.1063/1.4990440

View online: <http://dx.doi.org/10.1063/1.4990440>

View Table of Contents: <http://aip.scitation.org/toc/php/24/7>

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Laser pulse sharpening with electromagnetically induced transparency in plasma

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(Received 21 March 2017; accepted 13 June 2017; published online 6 July 2017)

We propose a laser-controlled plasma shutter technique to generate sharp laser pulses using a process analogous to electromagnetically induced transparency in atoms. The shutter is controlled by a laser with moderately strong intensity, which induces a transparency window below the cutoff frequency, and hence enables propagation of a low frequency laser pulse. Numerical simulations demonstrate that it is possible to generate a sharp pulse wavefront (sub-ps) using two broad pulses in high density plasma. The technique can work in a regime that is not accessible by plasma mirrors when the pulse pedestals are stronger than the ionization intensity. *Published by AIP Publishing.*

[<http://dx.doi.org/10.1063/1.4990440>]

I. INTRODUCTION

Short laser pulses are useful both because they can resolve transient phenomena and because they can reach higher intensities. The quest for a shorter pulse duration and higher signal-to-noise ratio of a laser pulse using lower-cost experimental techniques has stimulated a rich study in both solid-state lasers and plasma compressors.^{1–4} In particular, plasma amplifiers based on Raman or Brillouin scattering, in which a pump pulse continuously deposits its energy into a sharp seed pulse, promise to produce exawatt laser pulses.^{5,6} However, experimental realizations of such schemes are inhibited by the difficulty of preparing a sharp laser seed.²³

Currently, short pulses are usually generated with a mode-locked laser, but they suffer from poor contrast ratios. Optical parametric amplifiers (OPA) produce high quality pulses, but they require a more complicated phase-matching condition. For improving the temporal contrast ratio of short laser pulses, a commonly used technique is plasma mirrors (PM).^{7,8} A PM is made of a foil or glass target which, when ionized by a strong laser field, forms a layer of overdense plasma and abruptly reflects the laser pulse. Since the low intensity laser “prepulse” is not sufficiently strong to induce high plasma density, it is transmitted through the PM. However, PM only works with an ultrashort laser with a decent initial contrast. It can only suppress the pedestals that are below the ionization intensity, which is typically 10^{14} W cm⁻². It also requires that the pulse be shorter than a few picoseconds; otherwise, the sharp interface will be ruined by plasma expansion. Ionization costs a significant amount of the pulse energy and leaves a region that needs mechanical scanning or reconstruction. Therefore, preparing a sharp and clean laser pulse remains a challenge and continues to be the subject of active research.

Here, we propose an alternative scheme of generating sharp wavefronts by using two broad counter-propagating pulses with different frequencies in a high-density plasma slab. It uses a high-frequency pump laser to control the transmittance of a low-frequency seed laser in a high-density plasma slab—the plasma slab only abruptly lets the seed

laser transmit when the pump intensity exceeds a threshold value. This abruptness creates a sharp wavefront in the seed transmission. For nonrelativistic seed, the timing of the shutter is controlled solely by the strong pump and it does not depend on the seed intensity. The sharpness of the wavefront depends on the frequencies of the pump laser and the plasma, regardless of the initial duration or contrast ratio of the seed laser. Since the sharp wavefront is conditionally transmitted, it avoids the issue of plasma expansion or density fluctuation.

The mechanism of the proposed optical shutter is based on an analog of electromagnetically induced transparency (EIT)^{9–11} in atoms. Pump laser above threshold intensity can also induce a transparency window in a high density plasma for a seed laser that is below the “cut-off” frequency.¹² More comprehensive studies involving both the Stokes and anti-Stokes waves were conducted by Matsko and Rostovtsev,¹³ and Gordon *et al.*^{14,15} Our proposal makes use of the unique threshold behavior of EIT, which allows transforming the gradual variation of optical intensity into an abrupt transmittance. Susceptible to the optical nonlinearity, transmission of the seed beam then features a steep wavefront.

II. THEORETICAL MODEL

The optical shutter, as illustrated in Fig. 1, includes a high-density plasma slab with resonance frequency ω_{pe} and two counter-propagating lasers of the same polarization—a pump laser with frequency ω_0 and a seed laser with frequency ω_1 . The laser frequencies are chosen such that

$$\omega_0 - \omega_{pe} < \omega_1 < \omega_{pe} < \omega_0. \quad (1)$$

When the pump intensity inside the plasma slab is low, the plasma slab reflects the seed beam which is below the “cut-off” frequency. As the pump intensity exceeds a threshold value, an EIT window arises between $\omega_0 - \omega_{pe}$ and ω_{pe} ; hence, the plasma slab becomes transparent for the seed beam. The seed beam is abruptly let through, yielding a sharp wavefront. The duration of the pump beam has to be sufficiently long so that the EIT window remains open before the seed wavefront exits. During propagation, the sharpened

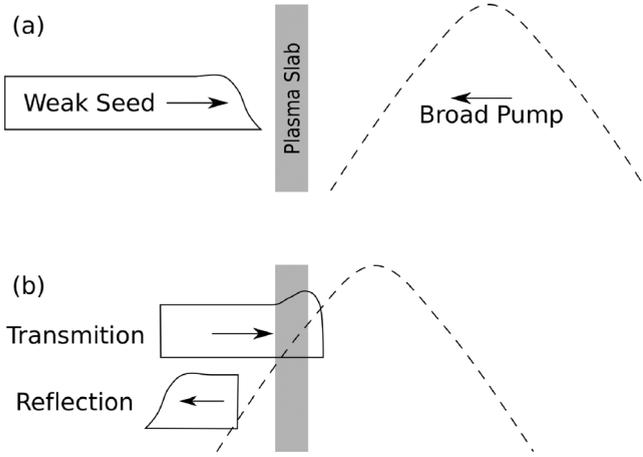


FIG. 1. Schematics of the optical shutter using two broad pulses with a high-density plasma slab. (a) A nonsharpened seed below the plasma “cut-off” frequency gets constantly reflected in the absence of pump in the plasma slab. (b) When pump intensity exceeds the threshold value, the seed is abruptly let through creating a sharp wavefront.

seed pulse, upon continued interaction with the pump, can be amplified and further steepened through a Raman-backscattering-like process.

Analogous to an atomic system, EIT in plasma arises from an interference effect enabled by the pump-driven plasma oscillation. When a laser beam propagates near the plasma surface, the electromagnetic wave drives electron motion in plasma. In the non-relativistic regime, electrons respond to the laser field instantaneously, i.e., for laser frequency below the plasma frequency ω_{pe} , the electrons oscillate at the laser frequency. In this case, the electron polarization has the same frequency but is out of phase with the incoming laser and hence, they destructively interfere, leading to reflection of the laser field. However, a transparency window can be induced if a pump laser is applied simultaneously. The pump and probe waves beat and their ponderomotive force produces a Langmuir wave, or a density ripple. The density ripple, driven at the difference of the applied laser frequencies, perturbs the electron polarization. Importantly, if the laser frequency difference is smaller than ω_{pe} , the phase of the perturbation opposes the primary electron polarization. This process induces a transparency window below the “cut-off” frequency and hence is called electromagnetically induced transparency.

The propagation and amplification of the seed beam can be analyzed using the dispersion relation. We model the coupling of the laser waves and the Langmuir wave in cold plasma with the conventional coupled three-wave equations

$$\left(\partial_{tt} - c^2 \partial_{zz} + \omega_{pe}^2\right) \mathbf{A}_0 = -\omega_{pe}^2 \frac{n}{\bar{n}} \mathbf{A}_1, \quad (2)$$

$$\left(\partial_{tt} - c^2 \partial_{zz} + \omega_{pe}^2\right) \mathbf{A}_1 = -\omega_{pe}^2 \frac{n}{\bar{n}} \mathbf{A}_0, \quad (3)$$

$$\left(\partial_{tt} + \omega_{pe}^2\right) \frac{n}{\bar{n}} = c^2 \partial_{zz} (\mathbf{A}_0 \cdot \mathbf{A}_1), \quad (4)$$

where \mathbf{A}_0 and \mathbf{A}_1 are the vector potentials of the pump laser and seed laser normalized to $e/m_e c$, respectively, with e being the natural charge, m_e being the electron mass, and c

being the speed of light. The electron density variation n/\bar{n} describes the Langmuir wave which oscillates at frequency $\omega_{pe} = \sqrt{\bar{n} e^2 / (\epsilon_0 m_e)}$, with ϵ_0 being the permittivity of vacuum. We first assume a weak initial seed and a nondepleted pump by neglecting dynamics of the pump [Eq. (2)]. The dispersion relation can then be exactly derived in the frequency regime^{13,14}

$$\omega_1^2 - c^2 \mathbf{k}_1^2 = \omega_{pe}^2 - f c^2 (\mathbf{k}_0 - \mathbf{k}_1)^2, \quad (5)$$

where $f = A_0^2 / [1 - (\Delta\omega/\omega_{pe})^2]$ with $\Delta\omega = \omega_0 - \omega_1$ being the two-photon detuning. Note that one cannot make $\Delta\omega = \omega_{pe}$ because it invalidates negligence of electron thermal velocity and damping. Compared with the normal dispersion relation of electromagnetic waves in plasma, Eq. (5) includes an extra term which depends on the pump intensity.

Conditions of transparency can be found by solving the dispersion relation [Eq. (5)] for \mathbf{k}_1 by setting ω_1 real. The solution can be expressed as

$$\left| \mathbf{k}_1 - \frac{f}{1-f} \mathbf{k}_0 \right| = \frac{1}{(1-f)c} \sqrt{f(\omega_0^2 - \omega_1^2) - (\omega_{pe}^2 - \omega_1^2)}. \quad (6)$$

The real roots of wavevector \mathbf{k}_1 lie on a circle centered at $f\mathbf{k}_0/(1-f)$. They become purely real so that the beam begins to propagate when the pump intensity is above the threshold value, i.e.

$$A_0^2 \geq A_{th}^2 \equiv \left[1 - \left(\frac{\Delta\omega}{\omega_{pe}} \right)^2 \right] \frac{\omega_{pe}^2 - \omega_1^2}{\omega_0^2 - \omega_1^2} \quad (7)$$

on the condition that $\omega_{pe} > \Delta\omega > 0$; otherwise, the inequality (7) is to be reversed. We show in Fig. 2(a) contour plot of the threshold value of pump amplitude A_{th} for EIT as a function of pump frequency ω_0 and seed frequency ω_1 . It is evident that a lower pump frequency enables a larger bandwidth

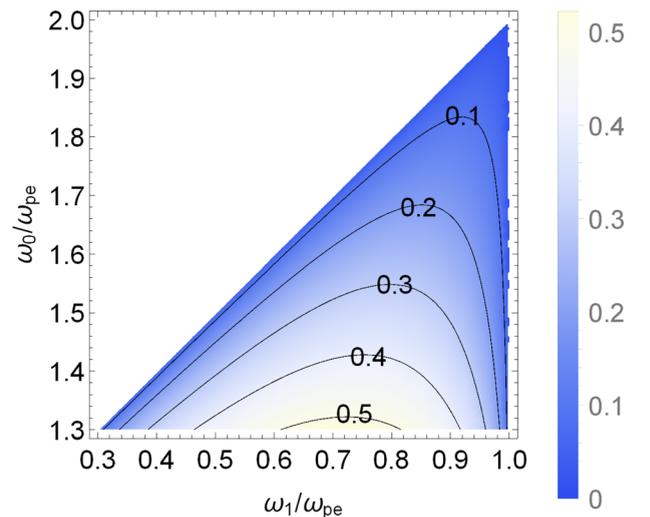


FIG. 2. Contour plot of the threshold value of pump amplitude A_{th} for EIT as a function of pump frequency ω_0 and seed frequency ω_1 normalized to plasma frequency ω_{pe} . In the presence of a pump, the EIT window (colored region) emerges at seed frequencies close to $\omega_0 - \omega_{pe}$ and close to ω_{pe} . Note that the EIT window does not exist in the blank region on top left.

of transparency window, but it also requires a higher threshold of pump amplitude. As an example of cases with a strong pump, we plot in Fig. 3(a) the real roots of k_1 assuming $k_1 \parallel k_0$. It shows that the transparency window, once opened, extends to $\omega_0 - \omega_{pe}$ which is below the “cut-off” frequency. Its spectra width is $\omega_{\text{EIT}} = 2\omega_{pe} - \omega_0$.

We note that the threshold value for EIT [Eq. (7)] does not depend on the directions of wavevectors, which allows us to use an arbitrary angle between the pump and seed beams. Although we focus on two counter-propagating lasers for simplicity of analysis and simulation, the flexibility might be an advantage in experiments as it avoids the issue of aligning two optical pulses.

Instabilities of the propagating seed beam can be found by analyzing the root ω_1 as a function of real wavevector k_1 . Under the condition $\omega_0 \leq 2\omega_{pe}$, the solution to Eq. (5) can be well approximated as

$$\omega_1 \cong \frac{1}{2}(\omega_0 + \omega_h - \omega_{pe}) \pm \frac{1}{2} \sqrt{(\omega_{pe} - \omega_0 + \omega_h)^2 - A_0^2 \frac{2\omega_{pe}^2(\omega_0^2 - \omega_{pe}^2)}{\omega_0\omega_h}}, \quad (8)$$

where $\omega_h = \sqrt{\omega_{pe}^2 + c^2k_1^2}$. When the pump amplitude is above the threshold value, roots of ω_1 become complex for real wavevectors k_1 , which indicates an instability in this region. An example is shown in Fig. 3(b). From the plot, we can see that the dispersion curves have two branches in the regions of large wavevector k_1 . They, respectively, correspond to the Stokes sideband of the pump at $\omega_0 - \omega_{pe}$ and a frequency up-shifted mode at ω_h . The latter mode has been studied by Wilks *et al.*¹⁶ in the scheme of flash ionization in which electromagnetic field couples to plasma wave when an overdense plasma is abruptly created. In the regions of small wavevector k_1 , these two branch couples and lead to an instability. The maximum growth rate of instability exists at a point with a negative wavevector and with a frequency between $\omega_h = \omega_{pe}$ and $\omega_h = \omega_0 - \omega_{pe}$. Hence, backward scattering in a long plasma eventually dominates the outputs.

The sharpened wavefront of the seed beam arises from the abrupt change of the plasma dispersion relation, since it is controlled by pump pulse intensity. When the EIT window opens, the Langmuir wave and seed beam excite each other and propagate. Since the dispersion relation of the seed

depends on the pump intensity, we analyze the seed beam dynamics by first concentrating on the linear stage where pump intensity remains a constant. In this regime, the monochromatic seed beam has a definite wavevector k_1 . Hence, we can take the envelope approximation and write $\tilde{A}_1 = \tilde{A}_1 e^{-i(\omega_1 t - k_1 z)}$ and $n = \tilde{n} e^{-i[\Delta\omega t - (k_0 - k_1)z]}$. Then, Eqs. (3) and (4) can be rewritten as

$$2i(\omega_1 \partial_t - c^2 k_1 \partial_z) \tilde{A}_1 = \omega_{pe}^2 \frac{\tilde{n}}{\bar{n}} \tilde{A}_0 + D_1 \tilde{A}_1, \quad (9)$$

$$2i\Delta\omega \partial_t \frac{\tilde{n}}{\bar{n}} = -c^2(k_0 - k_1)^2 \tilde{A}_0 \cdot \tilde{A}_1 + D_n \frac{\tilde{n}}{\bar{n}}, \quad (10)$$

where $D_1 = \omega_{pe}^2 + c^2k_1^2 - \omega_1^2$ and $D_n = \omega_{pe}^2 - \Delta\omega^2$ describe dispersion of the waves. The dispersion terms are negligible¹⁷ as long as values of \tilde{n}/\bar{n} and \tilde{A}_1 are both smaller than \tilde{A}_0 . As such, Eqs. (9) and (10) become the well-known coupled wave equations for describing the linear stage of Stimulated Raman Scattering (SRS).¹⁸ Note that an EIT process is different from SRS, although their dynamic equations have a similar form. This can be seen from the frequency relations; EIT requires a nonresonant pump $\omega_0 < \omega_1 + \omega_{pe}$ and SRS uses a resonant pump for the maximum growth rate. Actually, SRS does not exist in a plasma of above one quarter of the critical density, where EIT is operated. The solution to Eqs. (9) and (10) has been studied extensively and can be expressed by convolution of the seed with a first order associated Bessel function. In our case, the amplified seed features an exponentially growing wavefront with growth rate $\Gamma = \text{Im}(\omega_1)$. In the nonlinear stage, the growth rate begins to decrease when pump intensity begins to deplete at the seed peak. The seed tail even stops propagating once the pump intensity falls below the threshold value. However, the seed wavefront continues to grow and gets sharpened. Its sharpness, defined by the “rising-time” t_r , approaches the asymptotic value which is limited by the finite frequency bandwidth of the EIT window

$$t_r = \frac{1}{\omega_{\text{EIT}}} = \frac{1}{2\omega_{pe} - \omega_0}. \quad (11)$$

Therefore, in order to increase the maximum seed sharpness, the plasma frequency ω_{pe} is preferably set close to half the pump frequency ω_0 . In the most favorable regime with seed frequency $\omega_1 \sim \omega_0/2$, the rising edge of the obtained

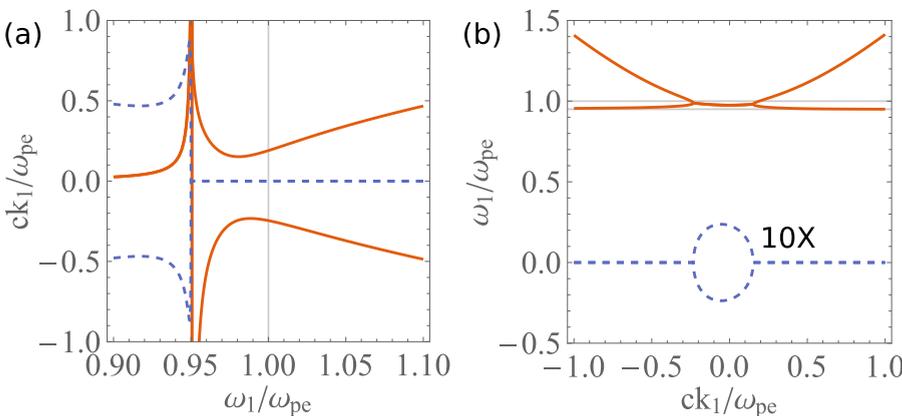


FIG. 3. The real (red solid) and imaginary (blue dashed) parts of the roots of the dispersion relation [Eq. (5)] at $A_0 = 0.04$. In (a), seed frequency ω_1 is set as real with wavevector k_1 being complex; in (b), seed wavevector k_1 is set as real with frequency ω_1 being complex. The dashed curve in (b) is multiplied by a factor of 10 for illustration purpose. The pump frequency is $\omega_0 = 1.95\omega_{pe}$ and its corresponding wavevector is $ck_0 = 1.67\omega_{pe}$. The thin gridlines show ω_0 and $\omega_0 - \omega_{pe}$ for reference. An EIT window and instability emerge between $\omega_0 - \omega_{pe}$ and ω_{pe} .

pulse only contains a small number of optical cycles, i.e., $\omega_1 t_r = 1/[2(\omega_{pe}/\omega_1 - 1)]$. Note that the input seed beam can be of any sharpness and even a continuous wave. Given a long plasma, the seed intensity can continue to grow. However, the seed also suffers strong group velocity dispersion (GVD) associated with the nonlinear dispersion relation which reduces pulse sharpness. Thus, a thin plasma slab is desirable for optimal sharpness of the pulse output. Its minimum thickness is confined by seed tunneling with a characteristic length $c/\sqrt{\omega_{pe}^2 - \omega_1^2}$. For higher pulse fluence, the sharpened pulse can be sent into a lower-density plasma medium for second stage amplification.

III. NUMERICAL SIMULATIONS

In order to demonstrate numerically this effect, we conduct full one-dimensional particle-in-cell (PIC) simulations using the code EPOCH.¹⁹ Two counter-propagating laser pulses are sent into a thin plasma slab with electron density $n_e = 1.14 \times 10^{20}/\text{cm}^3$ and correspondingly $\omega_{pe} = 2\pi \times 95.867$ THz. The left-going pump laser pulse has a frequency $\omega_0 = 1.95\omega_{pe} = 2\pi \times 187.50$ THz. The right-going seed pulse has a frequency $\omega_1 = 0.975\omega_{pe}$ which is below plasma frequency. Both of the laser pulses have the same Gaussian shape with a half width at half maximum (HWHM) of 0.59 ps (0.176 mm spatially). With this set of parameters, rising time of the sharpened seed would be limited to $t_r \approx 0.1$ ps. The threshold pump intensity for transparency at seed frequency is $I_{th} = 1.7\text{PW}/\text{cm}^2$ at which relativistic effect is negligible. We keep the temperature low (10 eV) to suppress Landau damping. A cell size of 4 nm is used to match the Debye length, and 300 electrons per cell are employed to reduce the charge density fluctuation. Ion motions are ignored in the simulation.

We present two snapshots of the simulation results in Fig. 4. Figure 4(a) shows the pulse envelopes (blue dashed for pump which propagates towards left and red solid for

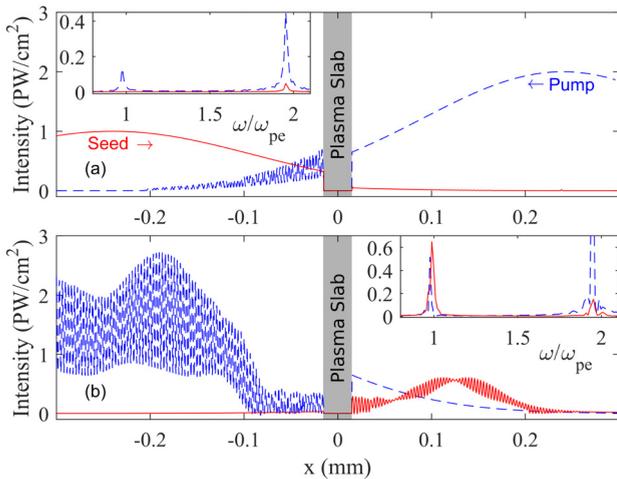


FIG. 4. PIC simulation of the laser pulses after (a) $t = 1.8$ ps and (b) $t = 3.2$ ps. The blue dashed and red solid curves show the envelopes of the pump and seed intensity, respectively. For illustration, the red curve in (a) is multiplied by a factor of 10. The inset shows spectra of the output (see main text for details). The weak broad seed pulse (HWHM = 0.59 ps) is compressed and amplified to a strong sharp pulse [HWHM = 0.15 ps shown in (b)].

seed which propagates towards right) at $t = 1.8$ ps before which the pump pulse intensity gradually grows but remains below I_{th} . We indeed do not observe any seed transmission in Fig. 4(a).²⁰ The inset shows frequency components of (i) right-propagating wave in the region $x > 0.03$ mm using a red solid curve; and (ii) left-propagating wave in the region $x < -0.03$ mm using a blue dashed curve. They are calculated using $\omega = 2\pi c/\lambda$ where λ 's are obtained by Fourier transforming the transmitted signal. The inset shows three peaks—peak of the red curve at pump frequency ($1.95\omega_{pe}$) is the reflection of pump beam on the plasma surface and peaks of the blue curve correspond to the transmitted pump and reflected seed, respectively. They beat producing the oscillation in the region between $x = -0.2$ mm and $x = -0.03$ mm. It shows no transmission at seed frequency ($0.975\omega_{pe}$).

As the interaction continues, the pump intensity grows above I_{th} . The EIT window then opens and the seed enters the plasma slab. The PIC simulation result at $t = 3.2$ ps is shown in Fig. 4(b). We first observe a strong and short amplified seed pulse between $x = 0.03$ mm and $x = 0.2$ mm. Its peak intensity reaches about $0.7\text{PW}/\text{cm}^2$ which is seven times stronger than the input seed. Its wavefront duration is strongly compressed to a HWHM of about 0.15 ps (0.04 mm spatially). The inset shows that the central frequency of the amplified seed is indeed below ω_{pe} . Oscillation in the transmitted seed arises from beating with the reflected pump. We also observe a strong beating signal in the transmitted pump, which confirms our theory that instability exists in both directions.

In the above “proof-of-principle” example, we notice the relatively high reflectance of the pump beam at the surface of the plasma slab. The reflected pump beam becomes a precursor and reduces the seed pulse contrast. According to the Fresnel reflection equation, the reflectance is

$$\mathcal{R} = \left| \frac{1 - \sqrt{1 - (\omega_{pe}/\omega_0)^2}}{1 + \sqrt{1 - (\omega_{pe}/\omega_0)^2}} \right|^2. \quad (12)$$

For the purpose of suppressing pump reflectance, higher values of ω_0/ω_{pe} are preferred. Note, however, that inequality $\omega_0 > \omega_1 + \omega_{pe}$ has to be obeyed, otherwise seed frequency falls outside the EIT window. An alternative means to suppress pump reflection is to introduce a density gradient close to the plasma surface. Functioning similar to an anti-reflection coating, the gradually varying plasma frequency can provide optical impedance matching²¹ and significantly minimize pump reflection. The corresponding PIC simulation result is shown in Fig. 5 where the plasma density profile is $n_e = 1.14 \times 10^{20} \times e^{-(x/30\mu\text{m})^2} \text{cm}^{-3}$. The amplified seed reveals an extremely sharp wavefront with a rise time of $t_r \sim 0.1$ ps, which agrees with Eq. (11) very well. Importantly, its front edge does not show any broad precursors. From the inset, we find that the reflected pump intensity is below 10% of the amplified seed; hence, the beating is negligible.

In order to distinguish the mechanism of pulse compression from the amplification process, we compare our results

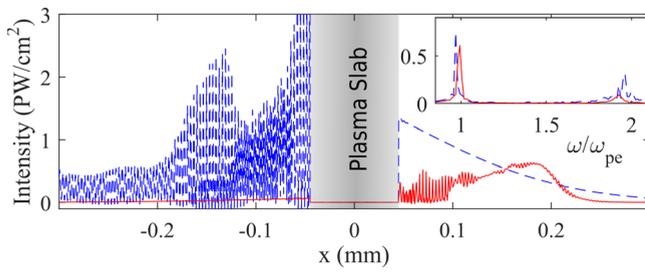


FIG. 5. PIC simulation results of the laser pulses $t = 2.7$ ps when the plasma density has a Gaussian distribution with $\text{HWHM} = 35.2 \mu\text{m}$. Other parameters are identical to those in Fig. 4. It shows that the pump reflection is strongly suppressed by the plasma density gradient.

with backward Raman amplification. We run a PIC simulation with the plasma density reduced by a factor of 2, so that $\omega_1 > \omega_{pe}$. The results show that transmission of the seed does not depend on the pump intensity, as expected. The transmitted seed contains a broad wavefront that is similar to the original seed. This is in contrast to the result using EIT which suppresses the precursors. Therefore, the simulations show that the threshold behavior of EIT is essential in pulse sharpening.

IV. CONCLUSION

We considered propagation of a seed laser pulse in an overdense plasma controlled by a separate pump pulse. When the pump intensity reaches a threshold value, it abruptly induces an EIT window for the seed pulse, yielding a sharp wavefront of the transmitted seed pulse. During propagation, the seed pulse gets amplified by a Raman-like parametric instability. The output intensity of the sharpened seed can be comparable to that of the pump. The sharpness of the obtained pulse is characterized by the “rise-time” of the pulse wavefront, i.e., $t_r = 1/(2\omega_{pe} - \omega_0)$. For optimal operation, the plasma slab should be thin enough to mitigate the GVD effect, but it should also be thicker than the characteristic length of seed tunneling ($c/\sqrt{\omega_{pe}^2 - \omega_1^2}$).

The threshold of pump amplitude, as expressed in Eq. (7), increases at a larger plasma frequency ω_{pe} which depends on plasma density and temperature. In a laser-induced plasma channel, finite plasma temperature often deteriorates plasma wave by increasing plasma frequency and Landau damping. These deleterious effects result in an increased threshold value and decreased growth rate of instability. Therefore, for given pump and seed pulses, random density fluctuation and finite temperature reduce the peak intensity of the obtained pulse. Nevertheless, the wavefront sharpness of the obtained pulse is immune to these deleterious effects. Since the seed frequency is below the plasma frequency, forward or side Raman scattering of the seed is automatically suppressed. Of interest in high-density plasmas is the Brillouin scattering of the pump beam due to the ion acoustic wave whose growth rate is approximately $\omega_{pi} = \omega_{pe} \sqrt{m_e/m_i}$ where m_e/m_i is the mass ratio of electron to ion. Using heavier ions would reduce the growth rate of this interaction, so that the ion wave would not reach significant amplitude within a thin plasma slab.

Note that one should not confuse EIT with relativistic transparency (RT)²² in plasmas. In RT, electrons, driven by superintense lasers, reach near light-speed and thus increase in mass. It slows the electron motion so that plasma can no longer shield the electromagnetic wave, and hence, transparency is induced. Although RT can also be used for pulse sharpening, it requires that the pulse itself be very intense (above 10^{18} – 10^{19} W cm^{-2}). Strong ponderomotive forces cause plasma expansion and the associated Doppler effect limits the pulse sharpness. In contrast, EIT arises from interference within the plasma wave interacting with different laser fields. This allows the use of weak pump lasers whose intensity can be well below the relativistic regime, e.g., 10^{15} W cm^{-2} .

ACKNOWLEDGMENTS

This work was supported by NNSA Grant No. DE-NA0002948, and AFOSR Grant No. FA9550-15-1-0391. The EPOCH code was developed as part of the UK EPSRC 300 360 funded project EP/G054940/1.

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